

Topologically Driven Coronal Dynamics - A Mechanism for Coronal Hole Jets

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Abstract. Bald patches are magnetic topologies in which the magnetic field is concave up over part of a photospheric polarity inversion line. A bald patch topology is believed to be the essential ingredient for filament channels and is often found in extrapolations of the observed photospheric field. Using an analytic source-surface model to calculate the magnetic topology of a small bipolar region embedded in a global magnetic dipole field, we demonstrate that although common in closed-field regions close to the solar equator, bald patches are unlikely to occur in the open-field topology of a coronal hole. Our results give rise to the following question: What happens to a bald patch topology when the surrounding field lines open up? This would be the case when a bald patch moves into a coronal hole, or when a coronal hole forms in an area that encompasses a bald patch. Our magnetostatic models show that, in this case, the bald patch topology almost invariably transforms into a null point topology with a spine and a fan. We argue that the time-dependent evolution of this scenario will be very dynamic since the change from a bald patch to null point topology cannot occur via a simple ideal evolution in the corona. We discuss the implications of these findings for recent Hinode XRT observations of coronal hole jets and give an outline of planned time-dependent 3D MHD simulations to fully assess this scenario.

1 Introduction

Magnetic bald patches are sections of a polarity inversion line (PIL) where the field lines are concave up rather than concave down as is the usual case for a loop geometry (a PIL is any location on the photosphere where the normal flux changes sign). The magnetic field lines forming a bald patch belong to a separatrix surface along which a current sheet

may be formed by shearing motions of magnetic footpoints at the photosphere (Low, 1987; Low and Wolfson, 1988; Wolfson, 1989; Vekstein et al., 1991; Vekstein and Priest, 1992; Karpen et al., 1990). Conditions for the appearance of bald patches at the solar surface were first described by Titov et al. (1993) and then extended by Bungey et al. (1996). A common flux distribution that leads to bald patch formation is that of a small opposite polarity region embedded in a large scale unipolar background field. Such a nested polarity will appear if, for example, a bipolar active region emerges in a unipolar hemisphere, or if an ephemeral region emerges in a coronal hole or if a small magnetic carpet bipole emerges in the unipolar network. Consequently, we expect this polarity distribution to be a generic feature of the solar photosphere.

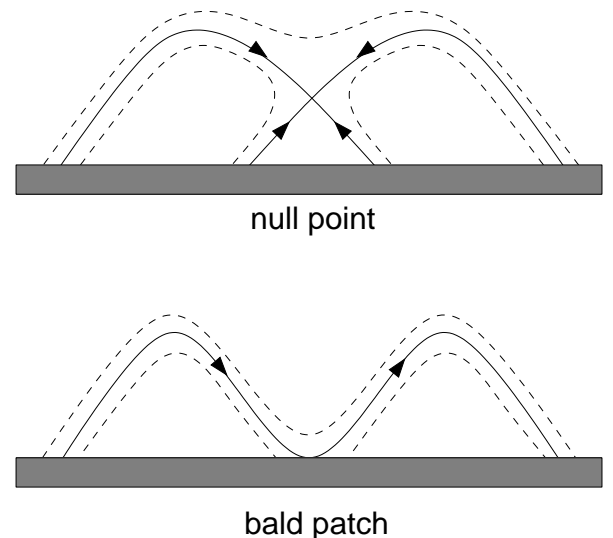


Fig. 1. Sketch of two different magnetic topologies: Null point (*top*) and bald patch (*bottom*).

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There are only two possible magnetic topologies for such a nested polarity region: Null points in the corona and magnetic bald patches. Figure 1 shows a sketch of these two topologies, while Fig. 2 shows a 3D rendering of field lines for both cases. Note that as long as there is only one nested polarity region, i.e. only one closed PIL in a large scale unipolar photospheric region, then the statements above must hold independent of the details of the distribution of the flux (Antiochos et al., 2007).

The best known and most widely studied topology of the two is that of a null point in the corona, along with the usual dome-shaped fan separatrix surface and pair of spine lines (e.g. Greene, 1988; Lau and Finn, 1990; Antiochos, 1990; Priest and Titov, 1996). On the other hand, a bald patch occurs if a null point is located below the surface such that it produces concave up field lines along part of the PIL. Determining the evolution of bald patch topologies is difficult, because simple line-tied boundary conditions cannot be used wherever the coronal field is concave up at the photosphere (Antiochos, 1990; Karpen et al., 1990). At the same time, bald patches are highly interesting since they are probably linked to jetting activity such as surges and sprays (Georgoulis et al., 2002). A bald patch topology was also found to be involved in surges by Mandrini et al. (2002), in a small flare (Aulanier et al., 1998), and in transition region brightenings (Fletcher et al., 2001). The primary goals of this paper are (a) to find out under which conditions magnetic bald patches exist, and (b) under which conditions existing bald patches are forced to vanish due to a change in the surrounding magnetic field.

We will describe our model and the methods in Sections 2 and 3, present some results in Section 4, establish a relation to recent Hinode XRT observations in Section 5, and finally discuss our findings in Section 6.

2 A simple magnetostatic model

Our model consists of a large global magnetic dipole and a small local embedded dipole which is placed slightly below the solar surface. The advantage of this simple configuration is that its magnetic potential, Φ , and field, $B = -\nabla\Phi$, can be calculated analytically. For a magnetic dipole with dipole moment \mathbf{d} at position \mathbf{r}_d and a source surface at $r = R_s$, the magnetic potential, Φ , at a location \mathbf{r} is given by (Antiochos et al., 2007)

$$\Phi = \frac{\mathbf{d} \cdot (\mathbf{r} - \mathbf{r}_d)}{|\mathbf{r} - \mathbf{r}_d|^3} - \frac{R_s r_d^3 \mathbf{d} \cdot (R_s^2 \mathbf{r} - r^2 \mathbf{r}_d)}{|r_d^2 \mathbf{r} - R_s^2 \mathbf{r}_d|^3}. \quad (1)$$

One can easily verify that $\Phi = 0$ at the source surface, $r = R_s$, i.e. the field is purely radial there. For the simplest case of a central dipole, Equation (1) reduces to

$$\Phi_0 = \frac{(\mathbf{d} \cdot \mathbf{r})(R_s^3 - r^3)}{R_s^3 r^3}. \quad (2)$$

The potential of a normalized central dipole can also be written as

$$\Phi_0 = \frac{1}{2R_s^3 + 1} \cdot r \cos(\theta) \cdot \left(\left(\frac{R_s}{r} \right)^3 - 1 \right). \quad (3)$$

The radial component of the magnetic field at the solar surface ($r = r_\odot = 1$) is then simply $B_r(\theta) = \cos(\theta)$. In this expression, θ denotes the co-latitude which is zero at the pole and $\theta = \pi/2$ at the equator.

If a dipole at a location \mathbf{r}_d is perpendicular to the radius vector, $\mathbf{d} \perp \mathbf{r}_d$, Equation (1) can be written as

$$\Phi_1(\mathbf{r}) = \frac{\mathbf{d} \cdot \mathbf{r}}{|\mathbf{r} - \mathbf{r}_d|^3} - \frac{\left(\frac{R_s}{r_d} \right)^3 \mathbf{d} \cdot \mathbf{r}}{\left| \mathbf{r} - \left(\frac{R_s}{r_d} \right)^2 \mathbf{r}_d \right|^3}. \quad (4)$$

The first term is the magnetic potential of the dipole, the second one is the potential of the corresponding image dipole. The image dipole is located at $\mathbf{r}_{\text{im}} = \left(\frac{R_s}{r_d} \right)^2 \mathbf{r}_d$ and has a dipole moment of $\mathbf{d}_{\text{im}} = -\left(\frac{R_s}{r_d} \right)^3 \mathbf{d}$. In this work, we consider a magnetic potential that is the sum of the potentials of a central dipole and a local dipole close to the surface, i.e.

$$\Phi = \Phi_0 + \Phi_1. \quad (5)$$

The addition of the local dipole results in a new PIL in addition to the one at the equator, which separates the nested polarity from its surroundings. Figure 3 illustrates the resulting large scale magnetic field for a source surface radius of $R_s = 2.5 r_\odot$ (this value is used throughout this work). The field lines outline the global dipole field structure, and the source surface is indicated by a gray wire mesh. The color shading of the solar sphere corresponds to the radial magnetic field strength, B_r .

We emphasize again that although the particular fields shown in Figs. 2 and 3 were derived for two dipole sources, the magnetic topology corresponds to any flux distribution that produces a global PIL and a small nested PIL.

3 Determining the separatrix between null point and bald patch solutions

As stated before, the primary goals of this study are to find out under which conditions magnetic bald patches exist, and under which conditions existing bald patches are forced to vanish due to a change in the surrounding magnetic field. As a first step, we constrain the problem by studying the conditions under which an embedded dipole supports a bald patch topology (which has a null point below the surface), and when there will be a null point above the surface.

To address this question, we carried out a parameter study by moving an embedded dipole via a sequence of equilibrium states from close to the solar equator to the pole. Its radial position $r_d = 0.94 r_\odot$ and its orientation in east-west direction parallel to the surface was kept constant. We then

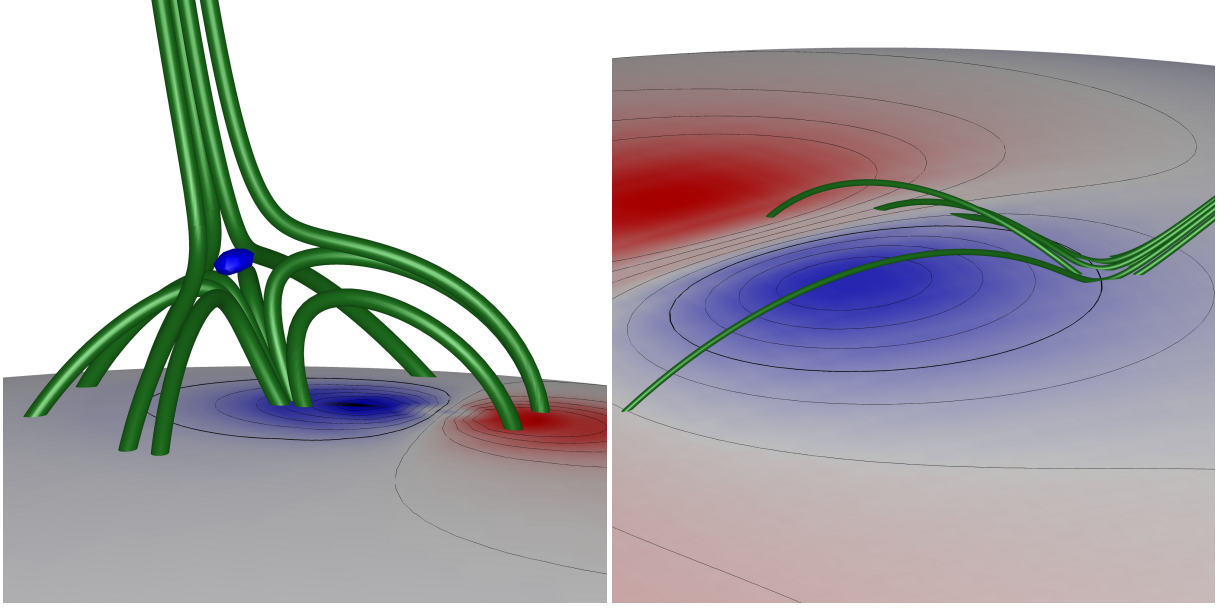


Fig. 2. A magnetic null point (*left*) and a bald patch topology (*right*). Red shading indicates positive, blue shading negative polarity of the radial magnetic field strength, B_r . The thick black lines indicate the polarity inversion lines (PILs), the blue bubble marks the location of the magnetic null point, and some magnetic field lines are drawn in green. For a bald patch topology, the magnetic null lies below the surface, and the field lines are parallel to the surface and concave up along part of the PIL.

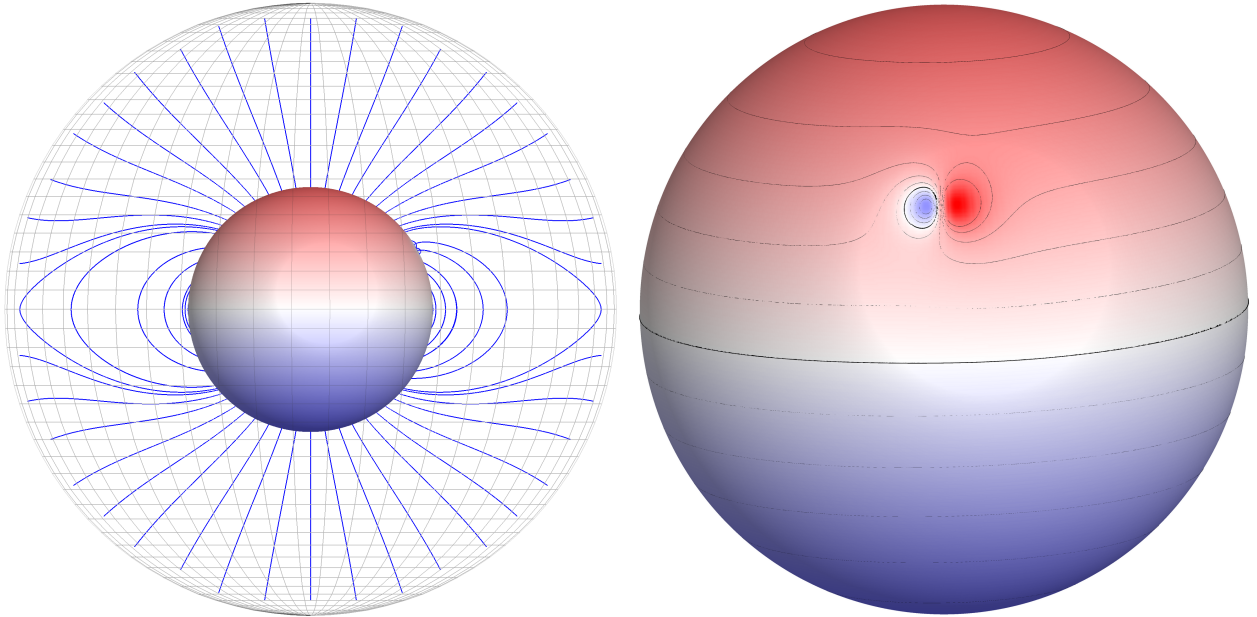


Fig. 3. Source surface model of the solar magnetic field. *Left panel:* The field lines outline the global dipole field structure, and the source surface is indicated by a gray wire mesh. The color shading of the solar sphere corresponds to the radial magnetic field strength. The magnetic bald patch shown in the right panel of Fig. 2 is located at the east limb around 30° northern latitude. *Right panel:* Same magnetic configuration, this time showing the bipolar structure that gives rise to the bald patch. The thin black lines represent iso-contours of the radial magnetic field, the thick black lines are the polarity inversion lines (PIL, $B_r = 0$).

determined the critical dipole strength, l_{crit} , that is needed to place the magnetic null right at the solar surface for all solar latitudes for which a closed patch of opposite polarity flux exists.¹ In general, for weak dipole strengths the null point will be submerged, while for larger values of l , the null point will be located above the surface. The dipole strength for which the magnetic null is exactly located at the solar surface will thus separate these two regimes and help to assess the physical conditions associated with each of them.

For a given latitude, this critical value of the embedded dipole strength is calculated by first determining the location, r_{min} , of the minimum of B^2 inside the discretized volume $\mathbf{B}(\mathbf{r}, l)$, and then minimizing the radial distance between the location of this minimum and the solar radius, r_{\odot} , i.e. finding the root of

$$f(B^2(\mathbf{r}, l)) = \underset{r}{\text{argmin}} (B^2(\mathbf{r}, l)) - r_{\odot}. \quad (6)$$

Since f is an implicit function of the dipole strength, l , this minimization is achieved using a modified Newton-Raphson method. In the expression

$$l_{n+1} = l_n - \alpha \frac{f(l_n)}{f'(l_n)} \quad (7)$$

of the conventional Newton-Raphson method, the analytical derivative is replaced by a numerical two-point derivative, and a convergence factor α is included and set to 0.5 (instead of the usual $\alpha = 1$) to avoid running into possible neighboring local minima of f . This as well as sufficiently high spatial resolution inside the computational domain are particularly important for a correct determination of the location of the null point since the global magnetic field decreases radially as r^{-3} .

4 Results

Figure 4 displays the magnetic flux enclosed by the PIL as a function of solar latitude for a null point at $r = r_{\odot}$. Combinations of latitude and dipole strengths that lie below this curve can support a bald patch topology, while those above will produce a null point above the surface. It can be seen that the amount of opposite polarity flux in the vicinity of a bald patch (i.e. the flux contained inside the associated PIL) decreases strongly with latitude. This means that an embedded dipole with a given surface magnetic flux can only give rise to a bald patch at latitudes below a critical value. For a relative flux of e.g. 0.01, the critical latitude is about 25° . Figure 5 shows the area of these nested polarities as a function of latitude. The shape of this curve is very similar to the one for the magnetic flux which indicates that the mean radial

¹Depending on the exact dipole strength and radial position, the PIL associated with the embedded dipole merges with the one that separates the two solar hemispheres around 15° latitude.

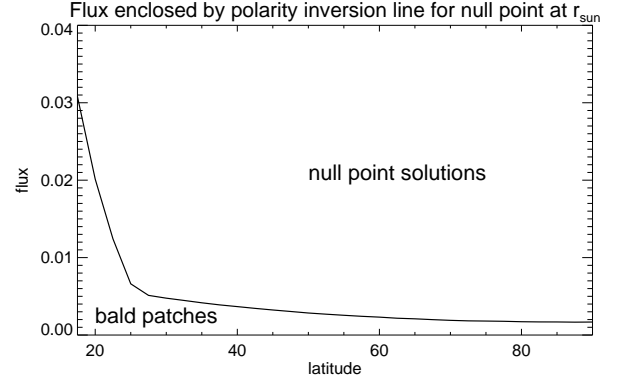


Fig. 4. Magnetic flux enclosed by PIL as a function of solar latitude for a null point at $r = r_{\odot}$. The plot shows that the amount of opposite polarity flux in the vicinity of a bald patch decreases strongly with latitude. This means that an embedded dipole with a given normalized surface magnetic flux of e.g. 0.01 can only give rise to a bald patch at latitudes of less than about 25° .

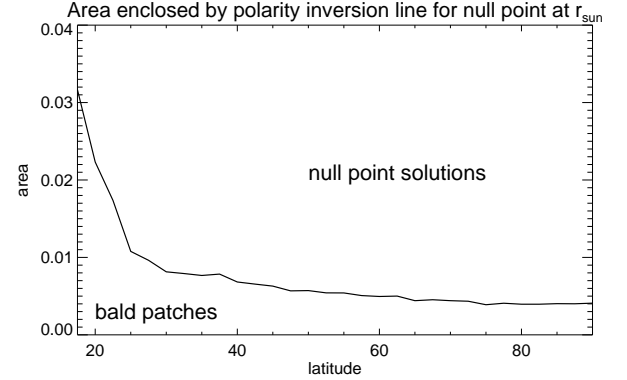


Fig. 5. Area enclosed by polarity inversion line as a function of solar latitude for a null point at $r = r_{\odot}$. This plot shows that large nested polarities only occur close to the equator.

magnetic field inside the nested polarities does not change substantially as a function of latitude. Finally, Fig. 6 shows the corresponding strength of the embedded dipole that is needed to place the magnetic null exactly at the solar surface. Taken together, these plots show that with increasing latitude, both the flux and size of nested polarities that are associated with bald patches strongly decrease. Already above 25 degrees latitude, the parameter regime in which we expect to find bald patches is very small, and especially inside a coronal hole (the approximate location of the coronal hole boundary is indicated in Fig. 6), we expect most embedded dipole to appear as null points in the corona instead of bald patches. To verify that the functional dependence found here is indeed the separator between null point and bald patch so-

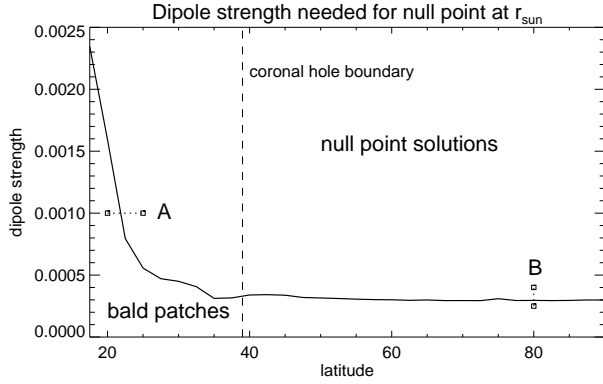


Fig. 6. Dipole strength needed to produce a magnetic null at the solar surface as a function of solar latitude. The squares connected by a dotted line indicate the two situations described in Sections 4.1 and 4.2.

lutions, we examined two specific cases which are marked "A" and "B" in Fig. 6.

4.1 Case A: Constant dipole strength

Keeping the dipole strength constant at $l = 0.001$, we inspected the field topology on both sides of the separator line. Figure 7 shows magnetic field lines around the PIL for latitudes of 20° (*left*) and 25° (*right*). As expected, we find a bald patch topology for 20° latitude (associated with the little square on the left hand side of the separator line in Fig. 6) and a null point for 25° latitude (associated with the little square on the right hand side of the separator line).

4.2 Case B: Constant latitude

In the second example, we kept the latitude of 80° fixed and varied the dipole strength from $2.5 \cdot 10^{-4}$ to $4 \cdot 10^{-4}$. Figure 8 shows magnetic field lines around the PIL for these two cases. Even for this high latitude close to the pole, we find a - very shallow - bald patch topology for the dipole strength that lies below the separator line ($l = 2.5 \cdot 10^{-4}$), while there is a null point for the dipole strength above the separator line ($l = 4 \cdot 10^{-4}$). This supports the earlier statement that the function $l_{\text{crit}}(\theta)$ which places the magnetic null right at the solar surface is indeed a separatrix between the two regimes. At first sight, the theoretical possibility of bald patches at and close to the solar pole seems slightly unexpected since one would not commonly associate this open-field region with a habitat for magnetic bald patches. However, Figs. 4 and 5 show that the corresponding nested polarity regions are very small and contain so little flux that they may easily be destroyed by the convective motions in the photosphere.

5 XRT Observations of Coronal Hole Jets

Recent observations with the X-Ray Telescope *XRT* on board the recently launched Hinode satellite frequently show coronal hole jets (Cirtain et al., 2007; Savcheva et al., 2007). These jets are very dynamic and relatively short-lived, and especially in their later stage often seem to outline a null point topology with a spine and a fan. We conjecture that these observations may be related to the transition from a bald patch to a null point topology. When the overlying field opens up or becomes sufficiently radial, a bald patch topology will transform into a null point topology. However, this process cannot take place smoothly in ideal MHD unless the submerged null point can emerge through the photosphere. This would mean, however, that concave up field lines that reach several scale heights deep into the convection zone would have to be lifted above the photosphere which seems unlikely given the amount of mass they carry. In these cases, we therefore expect violent coronal dynamics that could e.g. give rise to the observed coronal hole jets. Figure 9 shows an image of a northern polar coronal hole, taken with *XRT*'s Al/Poly filter. The dark shading corresponds to high intensity, the light shading to low intensity, and the arrows indicate two elongated structures inside the coronal hole which show jetting activity.

6 Discussion

Using a simple magnetostatic model, we have shown that magnetic bald patches of a significant size are likely to occur in closed-field regions close to the equator, but very unlikely to occur at higher latitudes, especially coronal holes. If bald patches encounter open-field surroundings, either by moving into a coronal hole or by the opening-up of the surrounding field, the bald patch topology almost invariably transforms into a null point topology with a spine and a fan. The time-dependent evolution of this scenario will be very dynamic since the change from a bald patch to null point topology cannot occur via a simple ideal MHD evolution in the corona. This mechanism of topologically driven dynamics may be important to understand the evolution of e.g. coronal hole jets such as those observed by Hinode's *XRT* instrument. Time-dependent 2D and 3D MHD simulations are planned to fully assess this scenario.

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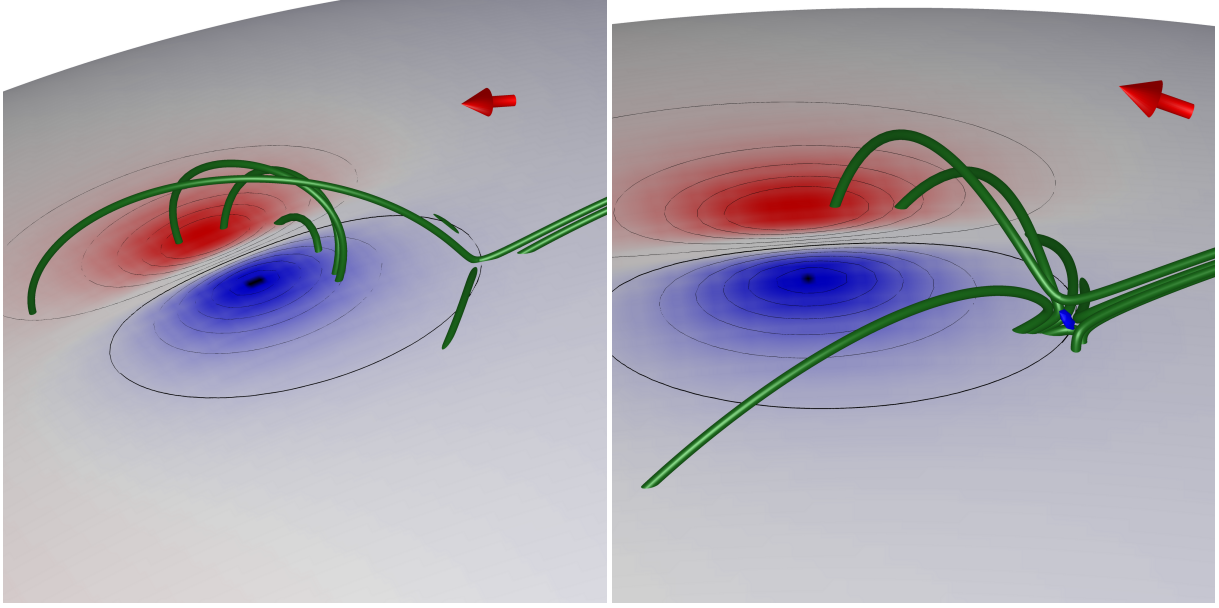


Fig. 7. Magnetic field lines around the polarity inversion line for 20° (left) and 25° latitude (right). The left plot shows a bald patch topology, while the right one shows a null point topology. The red arrows point north.

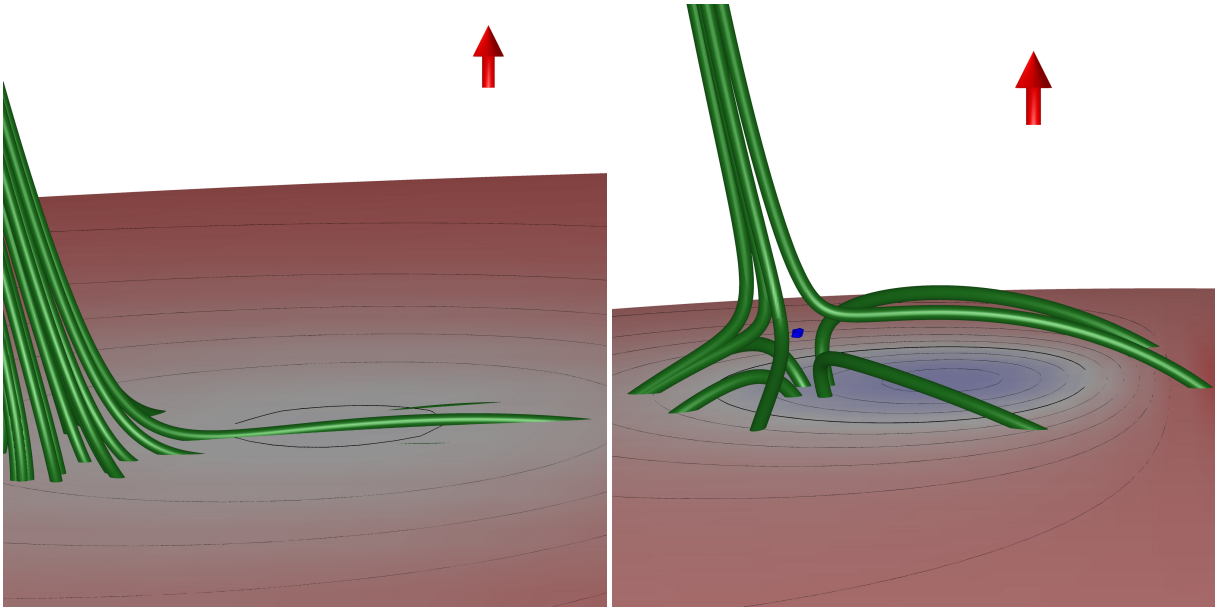


Fig. 8. Magnetic field lines around the polarity inversion line at 80° latitude (close to the pole) for dipole strengths of $2.5 \cdot 10^{-4}$ and $4 \cdot 10^{-4}$. The left plot shows a (very shallow) bald patch topology, while the right one shows a null point topology. The red arrows point north.

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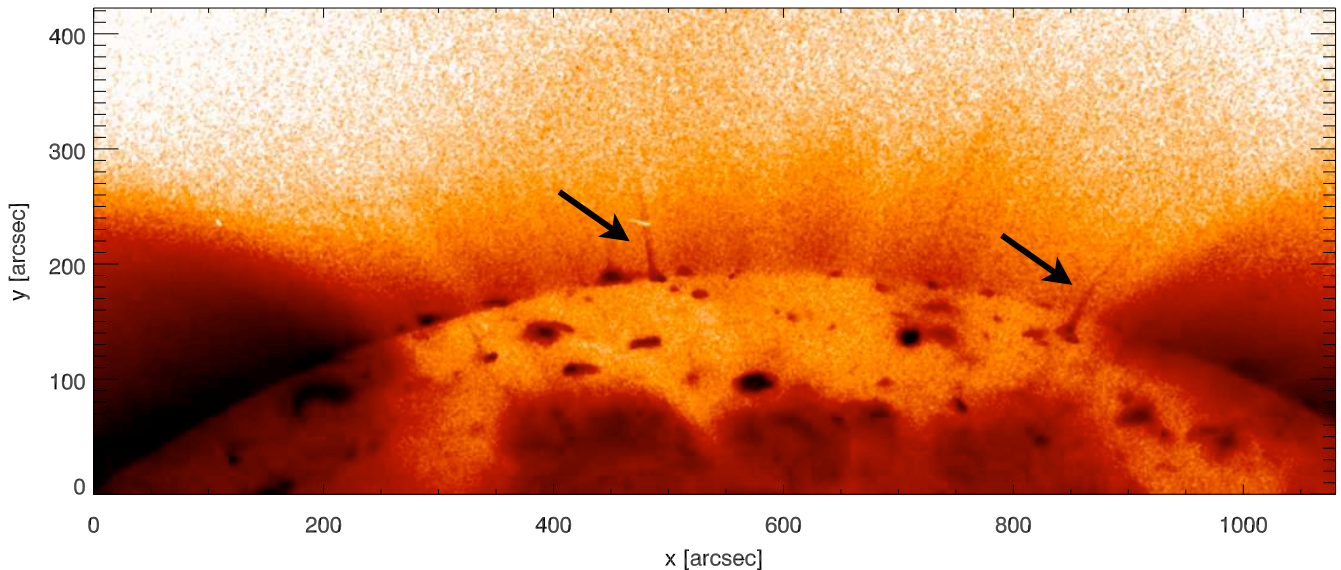


Fig. 9. Image taken by the X-Ray Telescope *XRT* on board *Hinode* on January 10, 2007 using the Al/Poly filter. The dark shading corresponds to high intensity, the light shading to low intensity. The arrows indicate two elongated structures inside the coronal hole which show jetting activity. *XRT* photo credit: JAXA/NASA/NAOJ/SAO.

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